Dear Students. The Mid-Term Exam (MTE) will be held on Monday, 14-th of April, at 17:00.

Part of the students will be allowed to pass the MTE distantly.

All students about the MTE procedure will be informed personally by e-mail either on-line or contactly.

Connection to the Zoom:

https://liedm.zoom.us/j/9999112448

Passcode: 12345678

Those who will participate contactly must to bring their own computers with installed all Octave software including installed my .m files.

Otherwise you must to install and launch Octave in class computer together with installed my .m files on them. During the MTE you must solve 2 problems:

1. Diffie-Hellman Key Agreement Protocol - DH KAP.

2. Man-in-the-Middle Attack (MiMA) for Diffie-Hellman Key Agreement Protocol - DH KAP.

The problems are presented in the site:

imimsociety.net

In section 'Cryptography':

Cryptography (imimsociety.net)

Please register to the site and after that you receive 10 Eur virtual money to purchase the problems. Please purchase and solve the only 1 problem at the time.

If the solution is successful then you are invited to press the green button [Get reward].

Then 'Knowledge bank' will pay you the sum twice you have paied.

So if the initial capital was 10 Eur of virtual money and you buy the problem of 2 Eur, then if the solution is correct your budget will increase up to 12 Eur.

You can solve the problems in imimsociety as many time as you wish to better prepare for MTE.

I advise you to try at first to solve the problem in 'Intellect' section to exercise the brains.

It is named as 'WOLF, GOAT AND CABBAGE TRANSFER ACROSS THE RIVER ALGORITHM'.

<<u>https://imimsociety.net/en/home/15-wolf-goat-and-cabbage-transfer-across-the-river-algorithm.html</u>>

The pictures of problems listed above are the following.



b.imimsociety.net

http://crypto.fmf.ktu.lt/telekonf/archyvas/inf5028-2025/

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On Monday, 18-th of March, 2025 was interesting Event about Post-Quantum Cryptography (PQC): https://www.youtube.com/watch?v=wjHR7TsYeEU



Asymmetric Encryption-Decryption: El-Gamal Encryption-Decryption

p=268435<mark>019</mark>; g=2;

Let message m^{\sim} needs to be encrypted, then it must be encoded in decimal number m: 1 < m < p. E.g. m = 111222. Then $m \mod p = m$.

27 mod 21 = 6 = 27 $P_{U}K_{A} = \alpha$ B: is able to encrypt m to R: m < p A: Ip-1 = {0, 1, 2, ..., p-2} *, + -mad(p-1) B: i - randi (Ip-1) $E = m \cdot q^{i} \mod p$ $D = q^{i} \mod p$ c = (E, D) - pA: is able to decrypt C=(E,D) using ber PrK=X. 1. $D^{-\times \mod (p-1)} \mod p$ $(- \times) \mod (p-1) = (0) - \times) \mod (p-1) =$ 2. $E \cdot D^{-x} mod p = m$ $=(\overline{P-1}-\times) \mod (P-1)$ $(p-1) \mod (p-1) = 0$, since $-\frac{p-1}{p-1} \quad \frac{p-1}{1}$ $(-x) \mod (p-1) = (p-1-x)$ $D^{-x} \mod p = D^{P-1-x} \mod p$ $>> D_m x = mod_{exp}(D, P-1-x, p)$ Encryption >> p=int64(268435019) >> x=int64(randi(p))>> m = 111222 p = 268435019 **x** = 131388089 m = 111222 >> dec2bin(p) >> a=mod exp(g,x,p) ans = 1111111111111111111001001011 a = 210917905 >> i=int64(randi(p)) >> g=2 i = 106367173 >> a_i=mod_exp(a,i,p) g = 2 a_i = 88353215 >> E=mod(m*a i,p)E = 220538197 >> D=mod exp(g,i,p)D = 134857055 Decryption 1) >> $m \times = mod(-X_2 p - 1)$ >> mx = mod(-x, p-1)mx = 137046929 2) >> $D_mx = mod_exp(D, mx_p)$ >> mod(x+mx,p-1) ans = 0>> D_mx=mod_exp(D,mx,p) $D_mx = 254989545$ >> mm=mod(E*D_mx,p) mm = 111222 Correctness

 $E_{nc}(P_{U}K_{A}=a,i,m)=c=(E,D)=(E=m\cdot a^{i}mod p;D=g^{i}mod p)$ $Dec(P+K_A=X, C) = E \cdot D^{X} \mod P = m \cdot \alpha^{i} \cdot (g^{i})^{-X} \mod P =$ $PuK = a = g^{x} \mod p$ $= m \cdot (g^{\mathbf{x}})^{i} \cdot g^{-i \mathbf{x}} = m \cdot g^{\mathbf{x}i} \cdot g^{-i \mathbf{x}} = m \cdot g^{\mathbf{x}i} \cdot g^{\mathbf{x}i} - i \mathbf{x} + m \cdot g^{\mathbf{x}i} -$ >> mod_exp(g,0,p) ans = 1 $= m \cdot 1 \mod p = m \mod p = m = 111222$ Since M < P

If $m > p \rightarrow m \mod p \neq m$; 27 mod $5 = 2 \neq 27$. ASCII: 8 bits per char. If $M ; 19 mod 31 = 19. <math>\frac{2048}{8} = 256 \text{ char.}$ Decryption is correct if m < p,

Authenticated Key Agreement Protocol using ElGamal Encryption and Signature. Hybrid encryption for a large files combining asymmetric and symmetric encryption method.

Hybrid encryption. Let *M* be a large finite length file, e.g. of gigabytes length.

Large file encryption - Hybrid encryption

Then to encrypt this file using asymmetric encryption is extremely ineffective since we must split it into millions of parts having 2048 bit length and encrypt every part separately.

The solution can be found by using **asymmetric encryption** together with **symmetric encryption**, say AES-128. It is named as **hybrid encryption method**.

For this purpose the **Key Agreement Protocol** (KAP) using **asymmetric encryption** for the same symmetric secret key **k** agreement must be realized and encryption of **M** realized by **symmetric encryption** method, say AES-128.

AKAP: Symmetric Enc & Asymmetric Enc & Digital Sign

Hybrid Encryption

How to encrypt large data file M: Hybrid enc-dec method. 1. Parties must agree on common symmetric secret key k. for symmetric block cipher, e.g. AES-128, 192, 256 bits.

Plaintext Plaintext Sender Plaintext Plaintext Plaintext Open Encrypt Communication Decrypt Channel Same key is used to encrypt and decrypt message Shared Secret Key B: PrKB=Y; PuKB=b. A: PrKA=X; PuKA=a. $P_{U}K_{A} = a.$ $P_{\mathcal{U}}K_{\mathcal{B}}=b.$ $\frac{1}{10} k \leftarrow randi(2^{128})$ $\frac{1}{10} k \leftarrow randi(2^{128})$ 1.1. Vorigy if RIK, and Certa are valid? $Enc(PuK_{B}=b, i_{k}, k)=c=(E, D)$ 1.2. Vorigy if 6 on h=H(G) is valid? 2) M- large file to be encrypted <u>c, G</u> 6, Puk_A h' = H(C) $E_k(M) = AES_k(M) = G$ Ver(Puka, 6, h') = Thue Cert 3) Signs ciphertext G 2. $Dec(PrK_{B}, c) = k$ 3. $D_k(G) = AES_k(G) = M$. 3.1) h = H(G) $s.2) \operatorname{Sign}(\operatorname{Pr}_{A}=\mathbf{X},h)=6=(r,s)$ A was using so called encrypt - and - sign (E-&-S) paradigm. (E-&-S)paradigm is recommended to prevent so called Choosen Ciphertext Attacks - CCA: it is most strong attack but most complex in realization. Till this place ElGamal encryption is probabilistic: encryption of the same message in two times yields the different cyphertexts C1 and C2.

in years under single and the superior of the second C1 and C2. 1-st encryption: 2-nd encryption $i_{2} \leftarrow randi(\mathcal{Z}_{p-n})$ $E_{2} = \mathfrak{M} \cdot \mathfrak{a}^{i_{2}} \mod \mathcal{P}$ $D_{2} = \mathfrak{g}^{i_{2}} \mod \mathcal{P}$ $\int \mathcal{C}_{2} = (E_{2}, D_{2})$ i, + i2 . in + randi (Zp-1) $E_{1} = (\underline{M} \cdot Q^{l_{1}} \mod p) C_{1} = (E_{1}, D_{4})$ $D_{1} = g^{l_{1}} \mod p$ $C_1 \neq C_2$

Necessity of probabilistic encryption.

Encrypting the same message with textbook RSA always yields the same ciphertext, and so we actually obtain that any deterministic scheme must be insecure for multiple encryptions. Tavern episode: competition, reward-bonus, jealousy Enigma:

		<i>i</i>	
Administrator	Alice	Bob c = (E, D)	Alice
> p=int64(268435019) p = 268435019 >> g=2	>> x=int64(randi(p-1)) x = 237315052 >> a=mod_exp(g,x,p)	>> m=111222 m = 111222 >> i=int64(randi(p-1))	>> mx=mod(-x,p-1) mx = 31119966 >>
g = 2 >> m=111222 m = <mark>111222</mark>	a = 47080507	i = 177611802 >> a_i=mod_exp(a,i,p) a_i = 105902610 >> E=mod(m*a_i,p)	>> D_mx=mod_exp(D,mx,p) D_mx = 95323339 >> mm=mod(E*D_mx,p) mm = <u>111222</u>
		E = 39890719 >> D=mod_exp(g,i,p) D = 138689606	